

# AI super-resolution-based models for turbulence and combustion

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## Predictive Large-Eddy Simulations (LESs)

- Fighting climate change requires many new/optimized technologies. E.g.:
  - more efficient engines
  - more efficient turbines
  - hydrogen as fuel
  - ammonia as fuel
- This is only efficiently possible with predictive simulations supporting the development and design process
- Data-driven subfilter models for LES

- Use high-fidelity direct numerical simulation (DNS) data to train data-driven subfilter models for complex LES
- Examples include simple turbulence data but also more complex data, such as breakup data used to model the fuel injection

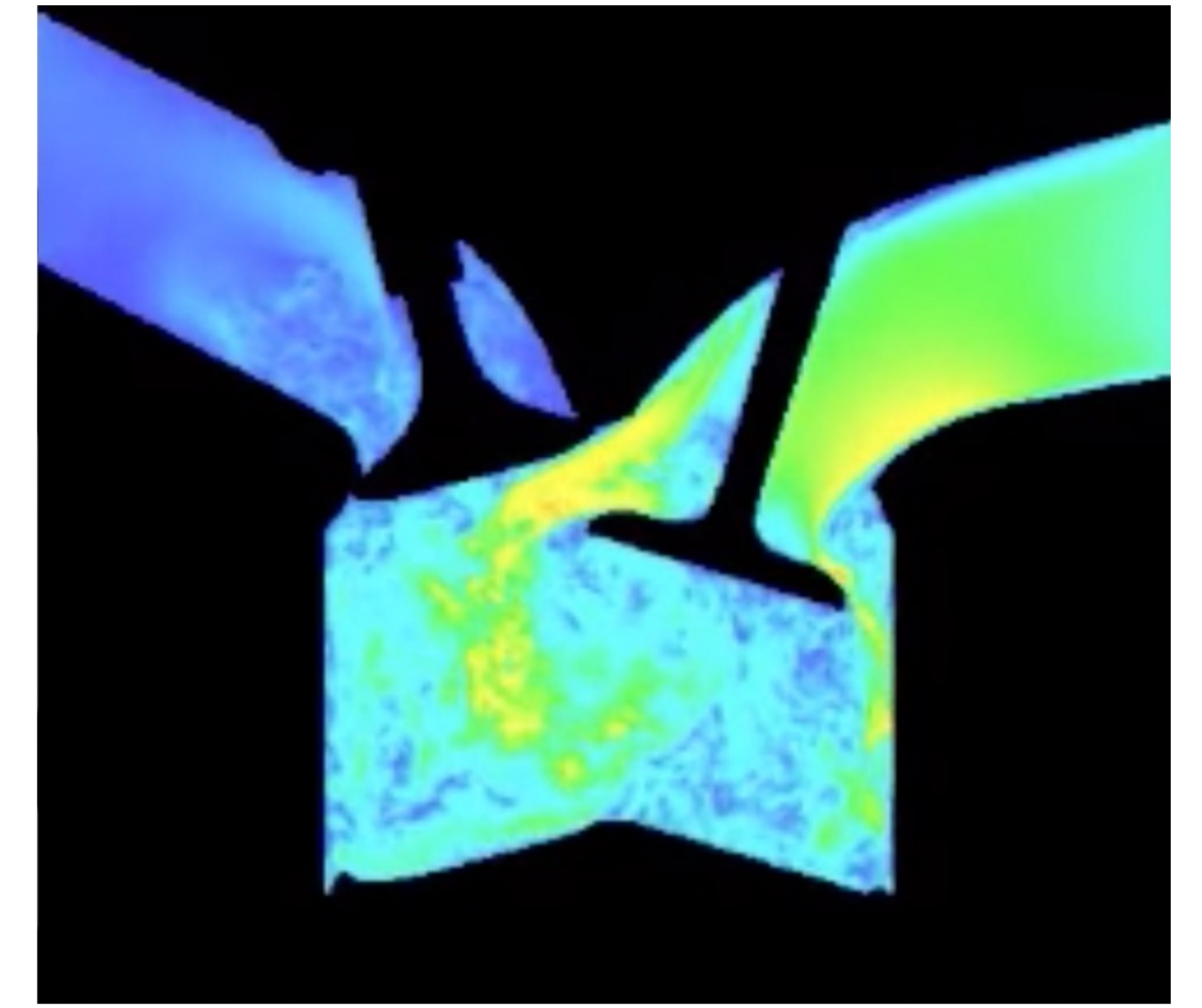


Fig. 1: Visualization of breakup DNS data (left) and complex engine LES (right). The highly-resolved DNS data can be used to train a data-driven subfilter model, which is then used to accurately model fuel injection in the LES.

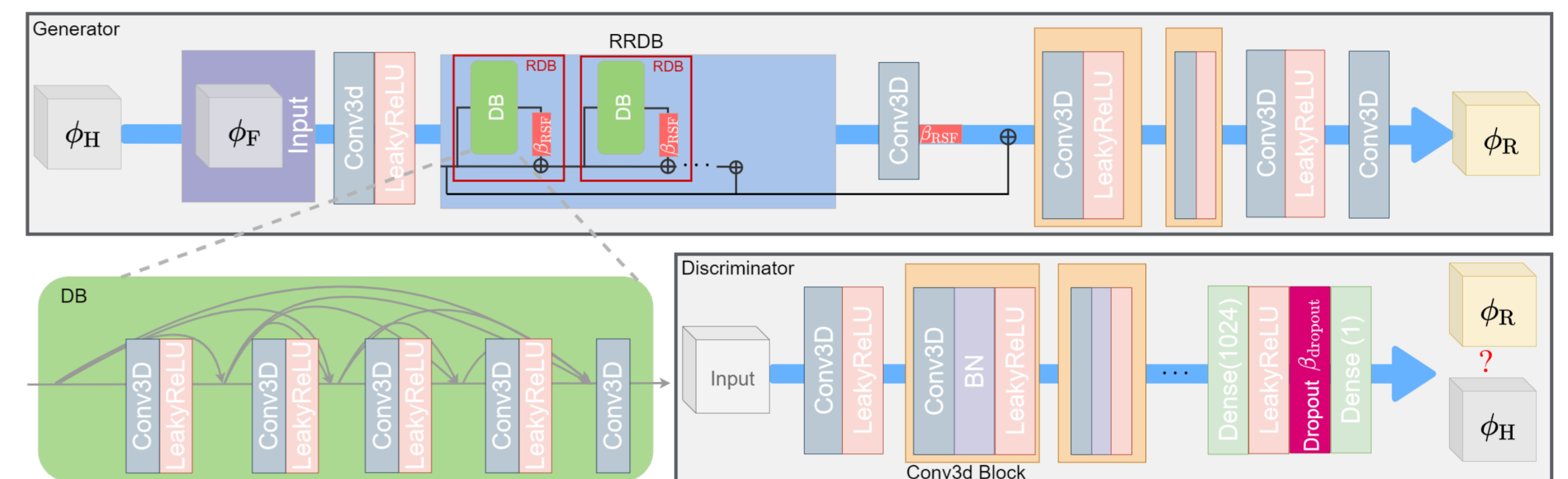
## Closing Algorithm

- Filtered/LES equations contain unclosed terms (red) which need to be modeled
- $$(\phi)_t + \mathbf{u} \cdot \nabla(\phi) = D\nabla^2(\phi) + \dot{\omega}_\phi$$
- $$\rightarrow (\tilde{\phi})_t + \mathbf{u} \cdot \nabla(\tilde{\phi}) = D\nabla^2(\tilde{\phi}) - \mathbf{u}'' \cdot \nabla(\phi'') + \tilde{\omega}_\phi$$
- Closure is done on reconstructed data fields which are generated by deep learning network called PIESRGAN

1. Use the PIESRGAN to reconstruct  $\Phi_R^n$  from  $\Phi_{LES}^n$ .
2. Use  $\Phi_R^n$  to update the primary species fields of  $\Phi$  to  $\Phi_R^{n;update}$  by evaluating the source terms and solving the unfiltered scalar equations on the mesh of  $\Phi_R^n$ .
3. Use  $\Phi_R^{n;update}$  to estimate the unclosed terms  $\Psi_{LES}^n$  in the LES equations of  $\Phi$  by evaluating the local terms with  $\Phi_R^{n;update}$  and applying a filter operator.
4. Use  $\Psi_{LES}^n$  and  $\Phi_{LES}^{n+1}$  to advance the LES equations of  $\Phi$  to  $\Phi_{LES}^{n+1}$ .

Alg. 1: AI super-resolution closing algorithm.

## Phys.-Informed Enhanced Super-Resolution GAN (PIESRGAN)

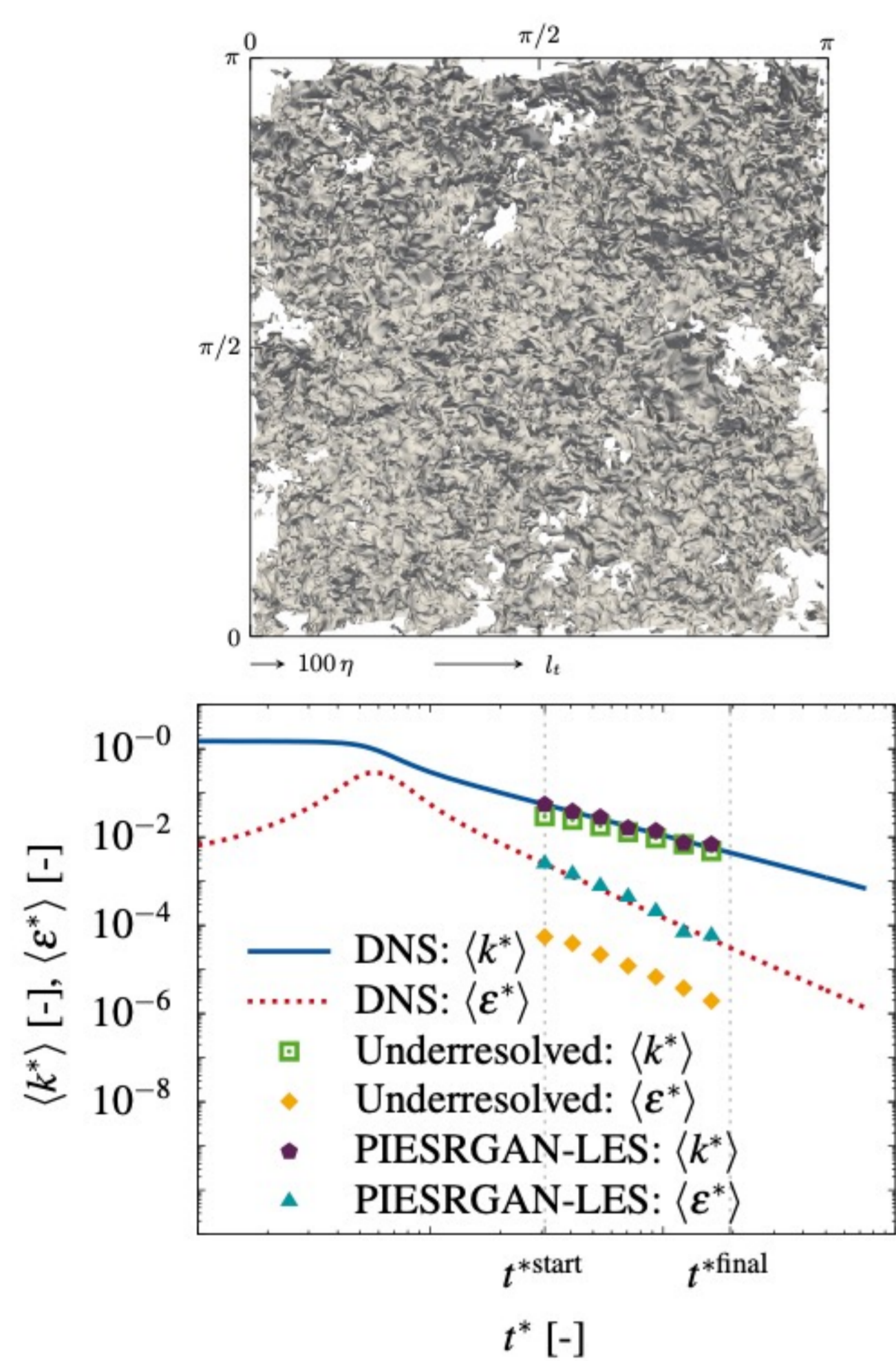


$$\mathcal{L} = \beta_1 L_{adversarial} + \beta_2 L_{pixel} + \beta_3 L_{gradient} + \beta_4 L_{physics}$$

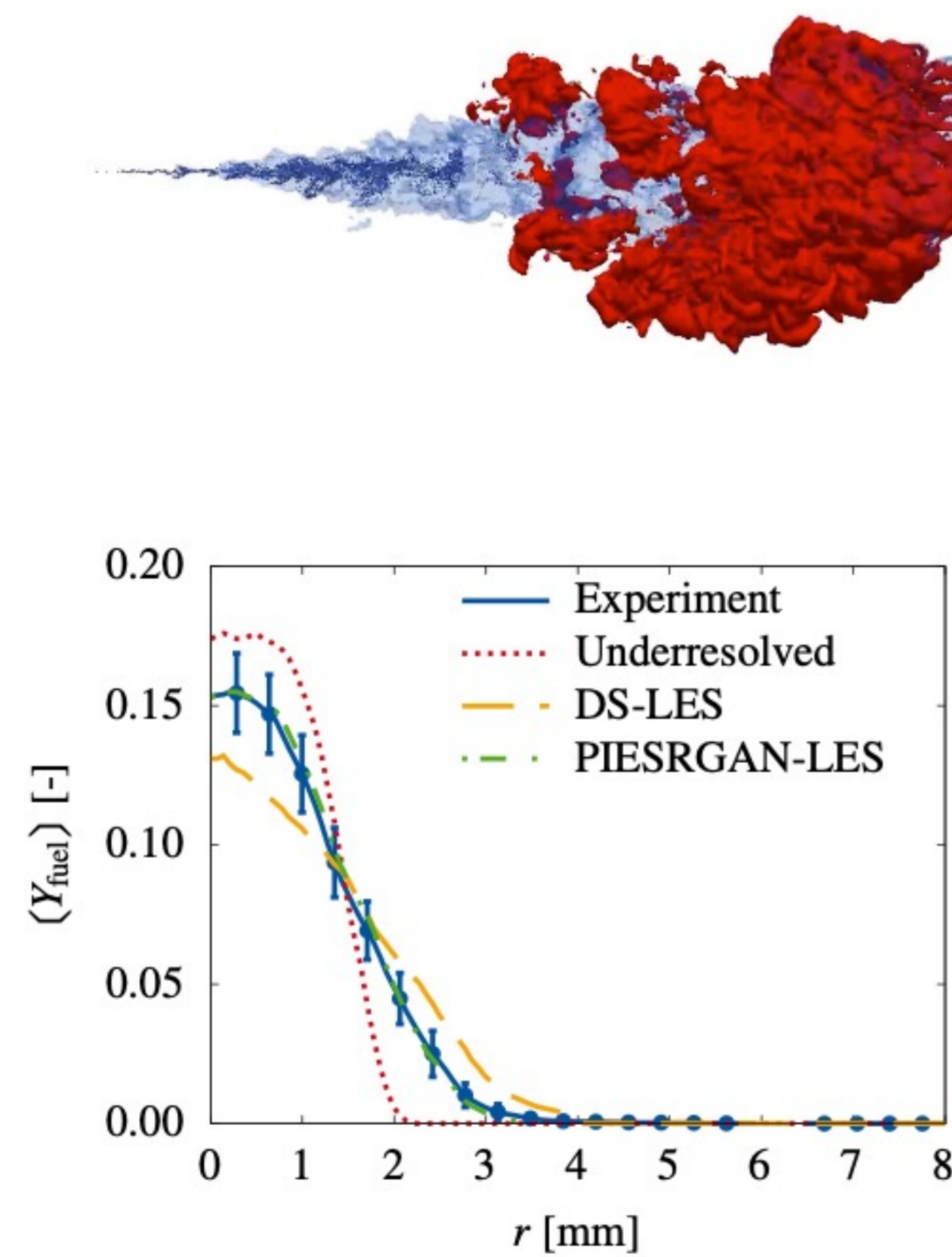
Fig. 2: Sketch of PIESRGAN and loss function.

## Results

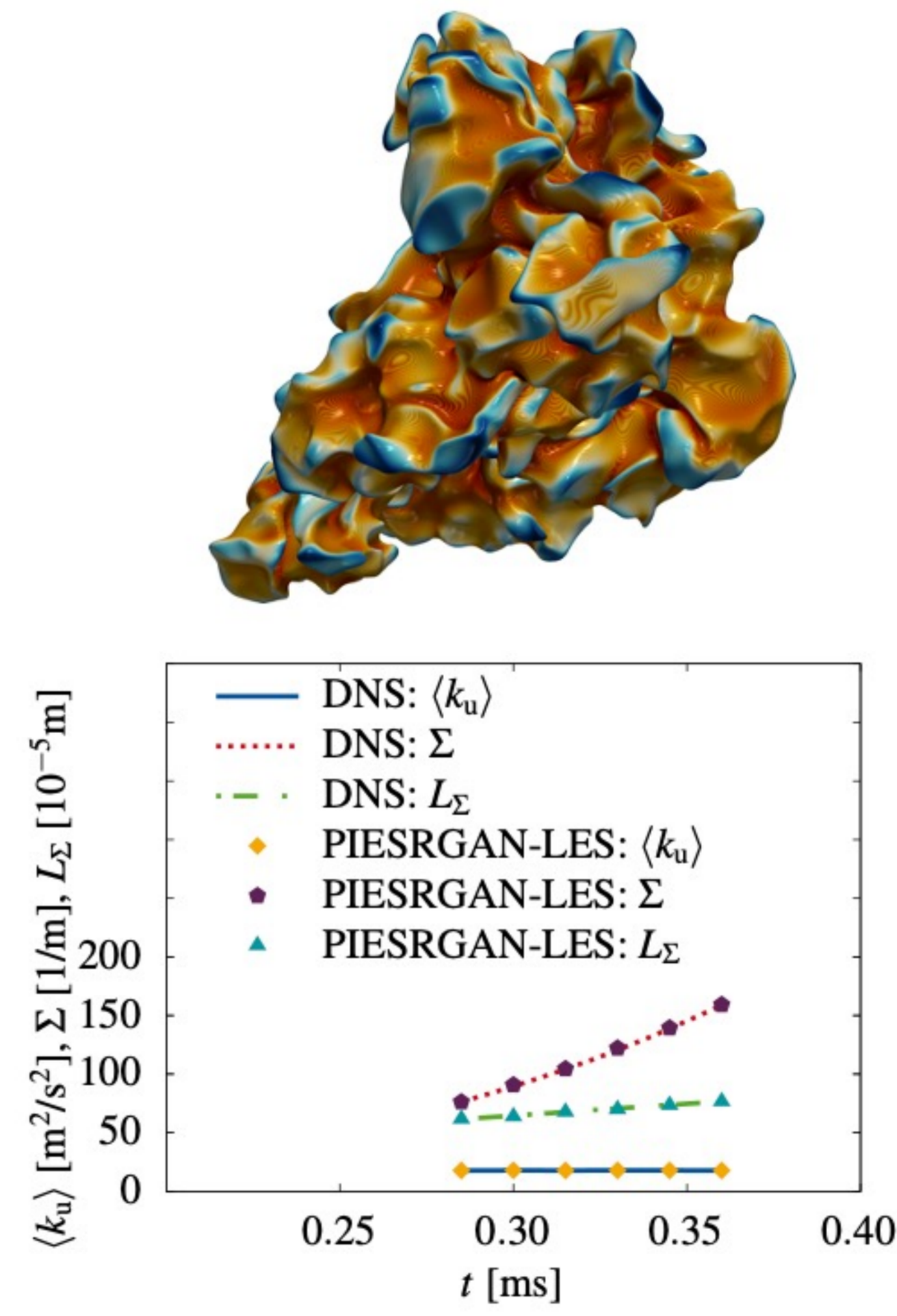
### Dec. turbulence



### Spray



### Premixed



### Non-Premixed

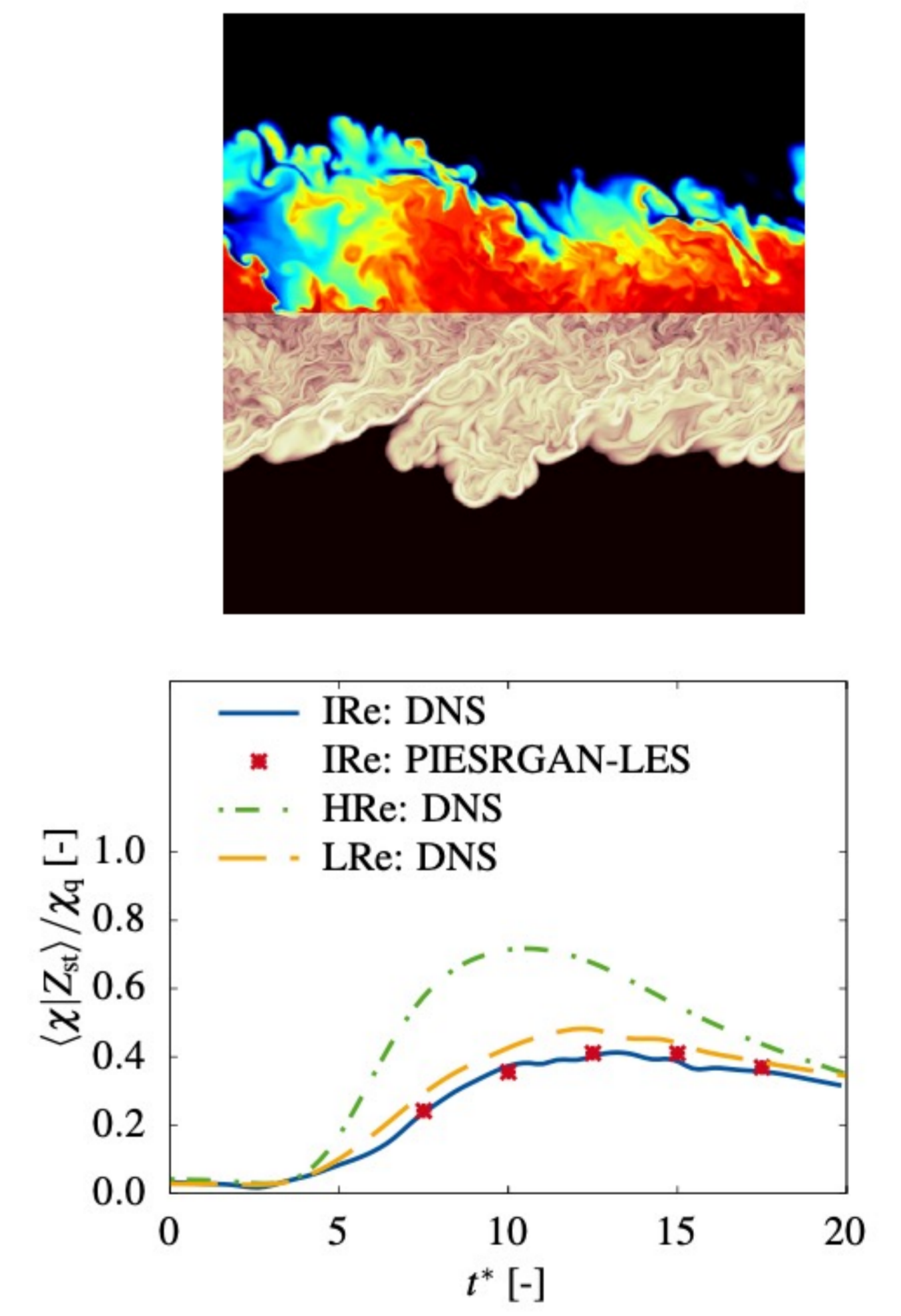


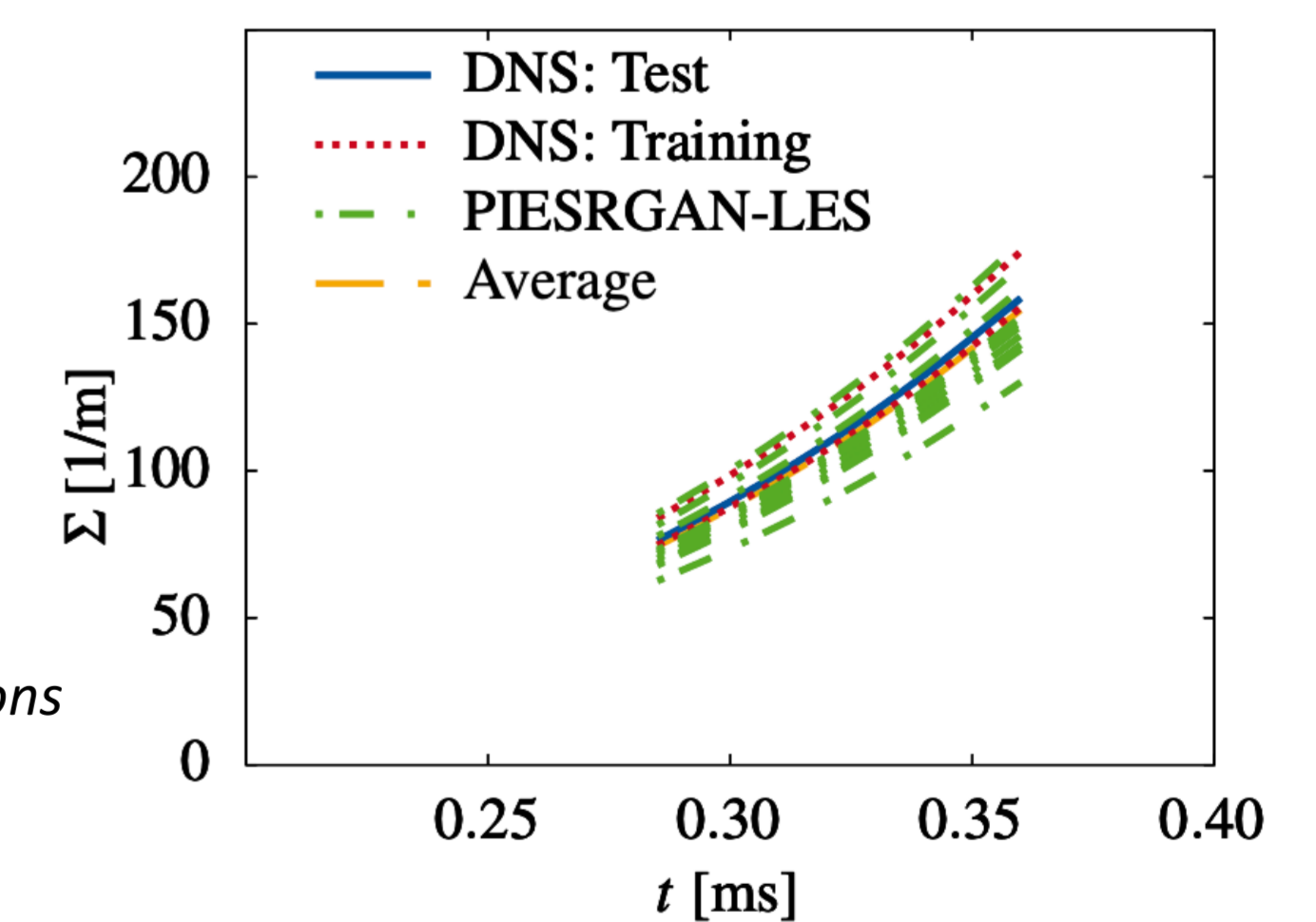
Fig. 3: Demonstration of PIESRGAN-subfilter accuracy in a posteriori tests of multiple complex flows.

## Achievements & Conclusions

- Generality
- Efficiency
- Robustness
- Accuracy
- “Universality”

- PIESRGAN was developed and applied to multiple complex flows
- PIESRGAN-LESs result in predictive simulations with higher accuracy than classical LES for lower computational cost on state-of-the-art supercomputers
- As example, cycle-to-cycle variation in engine flame kernels were computed with PIESRGAN-LES as simulations were cheaper than DNS
- Training convergence is still the main challenge and subject to current work

Fig. 4: Evaluation of cycle-to-cycle variations in engine flame kernels with PIESRGAN.



## References (selection)

- Bode et al., Using physics-informed enhanced super-resolution generative adversarial networks for subfilter modeling in turbulent reactive flows, PROCI, 2021
- Bode et al., Applying Physics-Informed Enhanced Super-Resolution Generative Adversarial Networks to Turbulent Premixed Combustion and Engine-like Flame Kernel Direct Numerical Simulation Data, PROCI, 2022
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- Bode, Applying Physics-Informed Enhanced Super-Resolution Generative Adversarial Networks to Turbulent Non-Premixed Combustion on Non-Uniform Meshes and Demonstration of an Accelerated Simulation Workflow, CNF (submitted)

## Acknowledgements

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